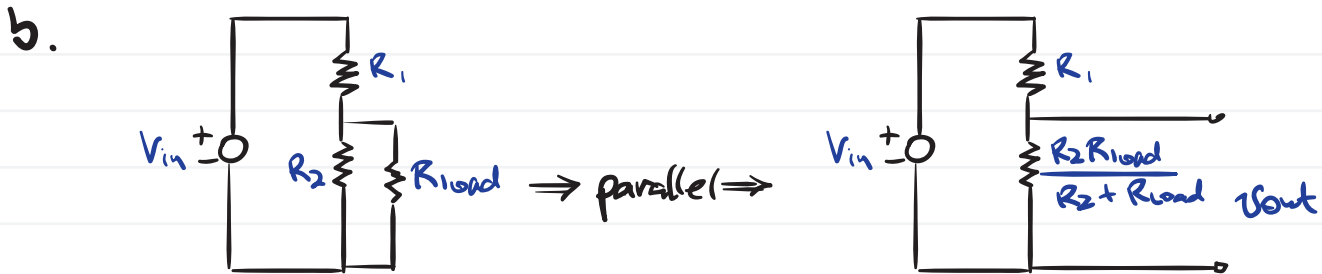


a. Voltage divider: $v_{out} = \frac{R_2}{R_1 + R_2} v_{in} = \frac{1}{2} (30) = 15 \text{ V}$ ✓



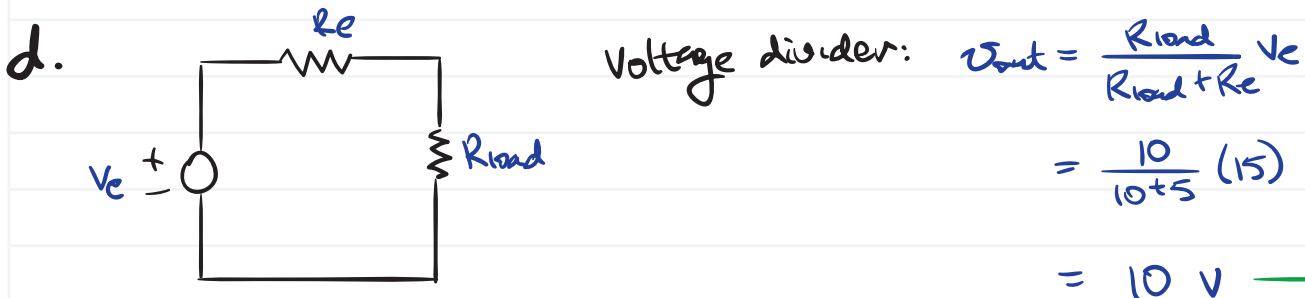
Now a voltage divider.

$$v_{out} = \frac{\frac{R_2 R_{load}}{R_2 + R_{load}}}{\frac{R_2 R_{load}}{R_2 + R_{load}} + R_1} v_{in} = \frac{R_2 R_{load}}{R_2 R_{load} + R_1 R_2 + R_1 R_{load}} v_{in}$$

$$= \frac{100 \text{ k}}{100 \text{ k} + 100 \text{ k} + 100 \text{ k}} (30) = 10 \text{ V}$$
 ✓

c. Thévenin eq.: $R_e = \frac{R_1 R_2}{R_1 + R_2} = 5 \text{ k}\Omega$ ✓

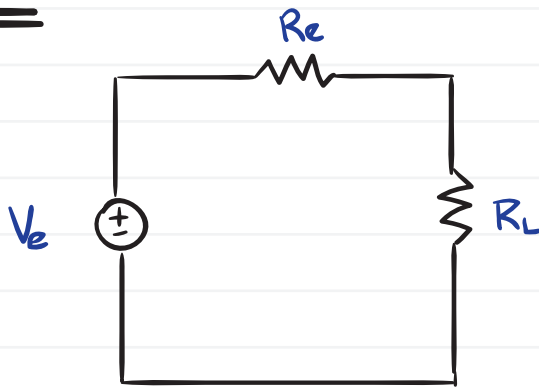
$$v_e = \frac{R_2}{R_1 + R_2} v_{in} = 15 \text{ V (voltage div.)}$$
 ✓



e. $P_{R_1} = v_{R_1}^2 / R_1 = \left(\frac{R_1}{R_1 + R_2} v_s \right)^2 / R_1 = 15^2 / (10 \cdot 10^3) = 22.5 \text{ mW}$ ✓

$$P_{R_2} = v_{R_2}^2 / R_2 = v_{out}^2 / R_2 = 10^2 / (10 \cdot 10^3) = 10 \text{ mW}$$
 ✓

$$P_{R_{load}} = v_{out}^2 / R_{load} = 10 \text{ mW}$$
 ✓



We want to maximize

$$P_L = U_{R_L}^2 / R_L.$$

$$\text{Voltage div.: } U_{R_L} = \frac{R_L}{R_e + R_L} V_e.$$

$$\text{So } P_L = \left(\frac{R_L}{R_e + R_L} V_e \right)^2 / R_L = \frac{R_L}{(R_e + R_L)^2} V_e^2$$

must be maximized in R_L .

$$\text{Differentiate: } \frac{\partial P_L}{\partial R_L} = \left(\frac{(R_e + R_L)^2 - 2R_L(R_e + R_L)}{(R_e + R_L)^4} \right) V_e^2$$

Set to zero and solve for R_L :

$$\left(\frac{(R_e + R_L)^2 - 2R_L(R_e + R_L)}{(R_e + R_L)^4} \right) V_e^2 = 0$$

$$(R_e + R_L)^2 = 2R_L(R_e + R_L)$$

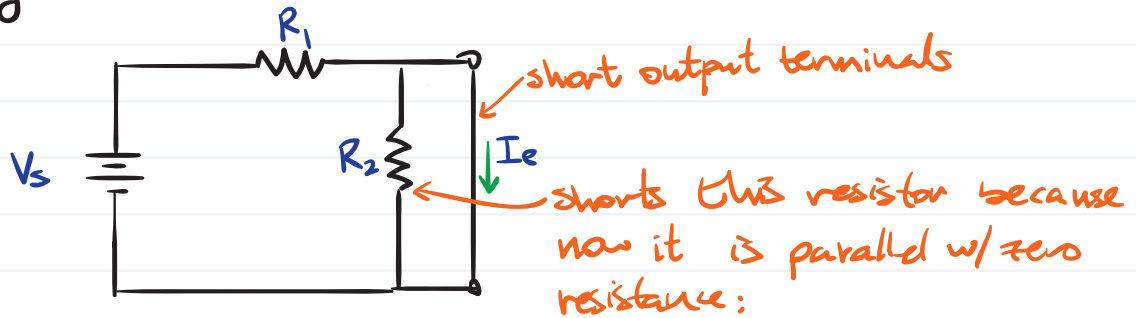
$$R_e = 2R_L - R_L$$

$$R_e = R_L \longrightarrow$$

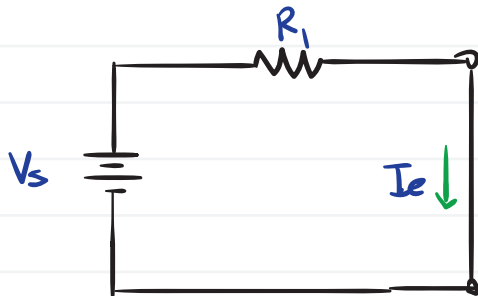
We should probably check that this is a max, not a min.

$$R_e = \frac{(10\text{K})(10\text{K})}{10\text{K} + 10\text{K}} = 5\text{K}\Omega$$

Finding I_e :



$$\frac{R_2 \cdot 0}{R_2 + 0} = 0 \text{ eq. resistance}$$



$$\begin{aligned} \text{So } I_e &= \frac{V_s}{R_1} = \frac{10}{10 \cdot 10^3} \\ &= 10^{-3} \text{ A} \\ &= 1 \text{ mA} \end{aligned}$$

There is also the loading part of the problem.